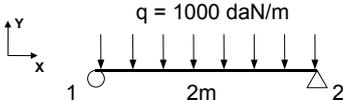
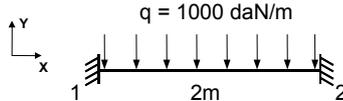
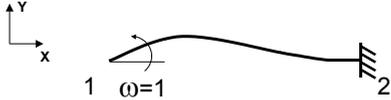


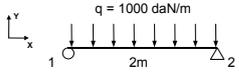
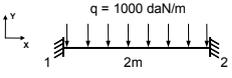
# - Méthode des déplacements -

- TP Rdm Le Mans

1/ Problème et résultats	2/ Système à degrés de liberté bloqués																					
 <p style="text-align: center;"><math>q = 1000 \text{ daN/m}</math></p> <p style="text-align: center;">1                      2m                      2</p> <p>Notations : indice 12 = action du nœud 1 sur la barre 12 indice 21 = action du nœud 2 sur la barre 12</p> <table style="margin-left: auto; margin-right: auto;"> <tr> <td><math>N_{12} =</math></td> <td style="border-left: 1px solid black; border-right: 1px solid black; width: 20px;"></td> <td><math>N_{21} =</math></td> </tr> <tr> <td><math>V_{12} =</math></td> <td style="border-left: 1px solid black; border-right: 1px solid black;"></td> <td><math>V_{21} =</math></td> </tr> <tr> <td><math>M_{12} =</math></td> <td style="border-left: 1px solid black; border-right: 1px solid black;"></td> <td><math>M_{21} =</math></td> </tr> </table> <p>Déplacements</p> <table style="margin-left: auto; margin-right: auto;"> <tr> <td><math>\omega_1 =</math></td> <td style="width: 100px;"></td> <td><math>\omega_2 =</math></td> </tr> </table>	$N_{12} =$		$N_{21} =$	$V_{12} =$		$V_{21} =$	$M_{12} =$		$M_{21} =$	$\omega_1 =$		$\omega_2 =$	 <p style="text-align: center;"><math>q = 1000 \text{ daN/m}</math></p> <p style="text-align: center;">1                      2m                      2</p> <p>Section de la poutre IPE 100</p> <table style="margin-left: auto; margin-right: auto;"> <tr> <td><math>N^{\circ}_{12} =</math></td> <td style="border-left: 1px solid black; border-right: 1px solid black; width: 20px;"></td> <td><math>N^{\circ}_{21} =</math></td> </tr> <tr> <td><math>V^{\circ}_{12} =</math></td> <td style="border-left: 1px solid black; border-right: 1px solid black;"></td> <td><math>V^{\circ}_{21} =</math></td> </tr> <tr> <td><math>M^{\circ}_{12} =</math></td> <td style="border-left: 1px solid black; border-right: 1px solid black;"></td> <td><math>M^{\circ}_{21} =</math></td> </tr> </table>	$N^{\circ}_{12} =$		$N^{\circ}_{21} =$	$V^{\circ}_{12} =$		$V^{\circ}_{21} =$	$M^{\circ}_{12} =$		$M^{\circ}_{21} =$
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$M^{\circ}_{12} =$		$M^{\circ}_{21} =$																				

3/ Système à déplacement unitaire imposé en 1	4/ Système à déplacement unitaire imposé en 2																		
 <p style="text-align: center;">1                      2</p> <table style="margin-left: auto; margin-right: auto;"> <tr> <td><math>N_{12} =</math></td> <td style="border-left: 1px solid black; border-right: 1px solid black; width: 20px;"></td> <td><math>N_{21} =</math></td> </tr> <tr> <td><math>V_{12} =</math></td> <td style="border-left: 1px solid black; border-right: 1px solid black;"></td> <td><math>V_{21} =</math></td> </tr> <tr> <td><math>M_{12} =</math></td> <td style="border-left: 1px solid black; border-right: 1px solid black;"></td> <td><math>M_{21} =</math></td> </tr> </table>	$N_{12} =$		$N_{21} =$	$V_{12} =$		$V_{21} =$	$M_{12} =$		$M_{21} =$	 <p style="text-align: center;">1                      2</p> <table style="margin-left: auto; margin-right: auto;"> <tr> <td><math>N_{12} =</math></td> <td style="border-left: 1px solid black; border-right: 1px solid black; width: 20px;"></td> <td><math>N_{21} =</math></td> </tr> <tr> <td><math>V_{12} =</math></td> <td style="border-left: 1px solid black; border-right: 1px solid black;"></td> <td><math>V_{21} =</math></td> </tr> <tr> <td><math>M_{12} =</math></td> <td style="border-left: 1px solid black; border-right: 1px solid black;"></td> <td><math>M_{21} =</math></td> </tr> </table>	$N_{12} =$		$N_{21} =$	$V_{12} =$		$V_{21} =$	$M_{12} =$		$M_{21} =$
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5/ Proportionnalités dans un système élastique linéaire																			
 <p style="text-align: center;">1                      2</p> <table style="margin-left: auto; margin-right: auto;"> <tr> <td><math>N_{12}</math></td> <td style="border-left: 1px solid black; border-right: 1px solid black; width: 20px;"></td> <td><math>N_{21}</math></td> </tr> <tr> <td><math>V_{12}</math></td> <td style="border-left: 1px solid black; border-right: 1px solid black;"></td> <td><math>V_{21}</math></td> </tr> <tr> <td><math>M_{12}</math></td> <td style="border-left: 1px solid black; border-right: 1px solid black;"></td> <td><math>M_{21}</math></td> </tr> </table>	$N_{12}$		$N_{21}$	$V_{12}$		$V_{21}$	$M_{12}$		$M_{21}$	 <p style="text-align: center;">1                      2</p> <table style="margin-left: auto; margin-right: auto;"> <tr> <td><math>K N_{12}</math></td> <td style="border-left: 1px solid black; border-right: 1px solid black; width: 20px;"></td> <td><math>K N_{21}</math></td> </tr> <tr> <td><math>K V_{12}</math></td> <td style="border-left: 1px solid black; border-right: 1px solid black;"></td> <td><math>K V_{21}</math></td> </tr> <tr> <td><math>K M_{12}</math></td> <td style="border-left: 1px solid black; border-right: 1px solid black;"></td> <td><math>K M_{21}</math></td> </tr> </table>	$K N_{12}$		$K N_{21}$	$K V_{12}$		$K V_{21}$	$K M_{12}$		$K M_{21}$
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6/ Superposition des systèmes										
 <p style="text-align: center;"><math>q = 1000 \text{ daN/m}</math></p> <p style="text-align: center;">1                      2m                      2</p>	$= \omega_1 ($  $) + \omega_2 ($  $) +$  <p style="text-align: center;"><math>q = 1000 \text{ daN/m}</math></p> <p style="text-align: center;">1                      2m                      2</p>									
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$N_{21} =$		$N_{21} =$								
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$M_{21} =$		$M_{21} =$								

7/ On vérifie les équations intrinsèques du système ( à quelques % près )					
Au nœud 1	Avec déplacements imposés		Au nœud 2	Avec déplacements imposés	
	en 1↓	en 2↓		en 1↓	en 2↓
$N_{12} =$	$\omega_1 N_{12} +$	$\omega_2 N_{12} +$	$N_{21} =$	$\omega_1 N_{21} +$	$\omega_2 N_{21} +$
$V_{12} =$	$\omega_1 V_{12} +$	$\omega_2 V_{12} +$	$V_{21} =$	$\omega_1 V_{21} +$	$\omega_2 V_{21} +$
$M_{12} =$	$\omega_1 M_{12} +$	$\omega_2 M_{12} +$	$M_{21} =$	$\omega_1 M_{21} +$	$\omega_2 M_{21} +$
		$N^{\circ}_{12}$			$N^{\circ}_{21}$
		$V^{\circ}_{12}$			$V^{\circ}_{21}$
		$M^{\circ}_{12}$			$M^{\circ}_{21}$